CALCULUS I, TEST I

MA 125-CW, CALCULUS I

February 8, 2016

Name (Print last name first):



Show all your work! No partial credit will be given for the answer only!

PART I

Part I consists of questions. Clearly write your answer in the space provided after each question. Show all of your your work!

All problems in Part I are 7 points each

Evaluate the following limits. <u>Question 1</u>

Use the **definition** of the derivative to show that the derivative of y = f(x) = 5x + 3 is f'(x) = 5.

<u>Question 2</u>

Find the derivative of $f(x) = x^2 \sin(x)$

Answer:

Question 3

Find the derivative of $y = f(x) = \frac{1-x^3}{1+x^3}$.

Answer:

<u>Question 4</u>

Find the derivative of $y = f(x) = \sqrt[5]{x}(x^3 + x^5)$.

Answer:

Question 5

Find the equation of the tangent line to the graph of $y = f(x) = \tan(x)$ at the point $a = \pi/4$.

Answer:

Question 6

Evaluate the limit $\lim_{\mathbf{x}\to\infty} \frac{\cos^3(x)+2}{x^5}$

Answer:

Question 7

Evaluate the limit $\lim_{x \to 5} \frac{x^2 - 2x - 15}{x^2 - 25}$

Answer:

PART II

Part II consists of 4 problems. You must show correct reasons to get full credit. Displaying only the final answer (even if correct) without the relevant steps will not get full credit.

Problem 1 (10 points)

Suppose that $S(t) = t^5 - 5t m$ is the position of a particle at time t (in seconds) on a line. Find:

(a) the velocity at time t.

(b) The displacement $S(t_2) - S(t_1)$ from $t_1 = 0$ to $t_2 = 2$.

(c) Is the **VELOCITY** increasing or decreasing when t = -1?

Problem 2 (10 points)

Given the graph of the function y = f(x) below find:

- 1. $\lim_{x \to -1^{-}} f(x) =$
- 2. $\lim_{x \to -1^+} f(x) =$
- 3. $\lim_{x \to -1} f(x) =$
- 4. $\lim_{x \to 2^{-}} f(x) =$
- 5. $\lim_{x \to 2^+} f(x) =$
- 6. $\lim_{x \to 2} f(x) =$
- 7. $\lim_{x \to \infty} f(x) =$
- 8. $\lim_{x \to -\infty} f(x) =$
- 9. State all intervals on which f(x) is continuous.
- 10. State all intervals where f(x) is differentiable.

Problem 3 (10 points)

Find all points on the graph of $f(x) = 2x^3 - x$ where the tangent line is parallel to the line y = 149x + 7.

Problem 4 (11 points)

Suppose $P(x) = \frac{100,000t}{t^2 + 100,000}$ (for $t \ge 0$) describes the profit (in dollars) from selling t items.

1. Given the definition of P(t), what is the meaning of P(2,000)?

2. Compute P'(2,000) and state what it means.

3. Considering your answer in (b), is your profit increased when you sell slightly more than 2,000 items?

Problem 5 (10 points)

Evaluate the following limits. Like always, justify your answers.

1. $\lim_{x \to \infty} \sqrt{x} + \sqrt{x+1}$



Scratch paper