Lecture 9: Chapter 9

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UAB Mathematics

24 October 2016

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• Women's mean body temperatures are lower than men's.

$$H_0: p_1 = p_2$$

> $H_0: p_1 = p_2$ $H_1: p_1 > p_2$

> $H_0: p_1 - p_2 = 0$ $H_1: p_1 - p_2 > 0$

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| Z-stat | $\hat{p_1}$ and $\hat{p_2}$ | p | E |
|--|---|---------------------------|--|
| $\frac{(\hat{p_1}-\hat{p_2})-(p_1-p_2)}{\sqrt{\frac{\bar{p}\bar{q}}{n_1}+\frac{\bar{p}\bar{q}}{n_2}}}$ | $\frac{x_1}{n_1}$ and $\frac{x_2}{n_2}$ | $\frac{x_1+x_2}{n_1+n_2}$ | $Z_{\frac{\alpha}{2}}\sqrt{\frac{\hat{p_1}\hat{q_1}}{n_1}+\frac{\hat{p_2}\hat{q_2}}{n_2}}$ |

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$$\hat{p_1} = \frac{28}{100} = 0.28, \ \hat{p_2} = \frac{35}{121} = 0.28926 \ \text{and} \ \bar{p} = \frac{28 + 35}{100 + 121} = 0.28507.$$

Thus, we have

$$z = \frac{-0.00926}{\sqrt{\frac{(0.28507)(0.71493)}{100} + \frac{(0.28507)(0.71493)}{121}}} = -0.15182.$$

Since z = -0.15182, we get that out *P*-value is $P(X \le -0.15182) = 0.4396$.

Since z = -0.15182, we get that out *P*-value is $P(X \le -0.15182) = 0.4396$. Because the *P*-value is greater than α , we fail to reject our null hypothesis. This means that there is **not enough evidence to support the claim** that $p_1 < p_2$, i.e. our original claim (that it's more likely for someone to spend money when given four quarters than when given a dollar bill) is not supported by this data.

We can do this in StatCrunch as well! Let's try testing this same hypothesis by constructing a confidence interval for $p_1 - p_2$ in StatCrunch!

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We can do this in StatCrunch as well! Let's try testing this same hypothesis by constructing a confidence interval for p_1-p_2 in StatCrunch! The 90% confidence interval we get is (-0.11, 0.09). Notice, this interval contains 0, which was our null hypothesis. Thus, we do not reject the null hypothesis, just as before. Note: The significance of the hypothesis test corresponding to this 90% CI is not 10%. What is it?

Finally, we could test the hypothesis using the critical value method.

Finally, we could test the hypothesis using the critical value method. The Z-stat from above was z = -0.15182. Because the left-tailed critical value corresponding to $\alpha = 0.1$ is -1.28, we see that the Z-stat does not lie beyond the critical value, and so we do not reject the null hypothesis, just as before.

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The samples both come from a normally distributed population or are samples with size more than 30.

Both samples are independent simple random samples.

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See pages 455-6, 459-60, and 468-9 for details!

Researchers conducted a study to determine if olive oil was antibacterial. The first sample consisted of 12 cultures treated with olive oil. The mean number of bacteria in the olive oil cultures was 0.57 million, with a standard deviation of 0.54 million. The second sample consisted of 12 untreated cultures. The mean number of bacteria in the untreated cultures was 0.67 million with standard deviation of 0.89 million. Assume that the populations of bacteria in these cultures in normally distributed.

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 $H_1: \mu_1 < \mu_2$

$\S9.3$ Claims About Two Independent Sample Means

We have

| | Sample 1 | Sample 2 |
|----------------|----------|----------|
| \overline{x} | 0.57 | 0.67 |
| S | 0.54 | 0.89 |
| n | 12 | 12 |

And we use a T-stat with unpooled variance, getting t = -0.333 and P = 0.3716.

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| | Sample 1 | Sample 2 |
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| x | 0.57 | 0.67 |
| 5 | 0.54 | 0.89 |
| n | 12 | 12 |

And we use a *T*-stat with unpooled variance, getting t = -0.333 and P = 0.3716. Thus, we fail to reject the null hypothesis. There is not enough evidence to support the claim that the average number of bacteria in a culture treated with olive oil is less than the average number of bacteria in a culture left untreated.

A candy manufacturer makes blue candies and red candies. They are made on the same machinery which ensures that they vary in size by the same amount. But they are made of different material, so the manufacturer is unsure which is heavier. She suspects they have the same weight. She samples 301 blue candies and 205 red candies, discovering that they have a mean weight of 1.50 grams and 1.40 grams respectively and standard deviations of 0.049 and 0.051 grams respectively. Test this claim with significance $\alpha = 0.01$. Use a confidence interval.

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$$H_0:\mu_1-\mu_2\neq 0$$

$\S9.3$ Claims About Two Independent Sample Means

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|---|----------|----------|
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| 5 | 0.049 | 0.051 |
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And we use a T-stat with pooled variance, getting the confidence interval (0.08,0.11).

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 Fifteen voters in Ohio and fifteen voters in Indiana have their IQs tested.

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Fifteen pairs of brothers and sisters have their IQs tests.

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- Fifteen pairs of brothers and sisters have their IQs tests.
- The first are independent and the second are dependent.

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■ *d*, the difference between two pairs

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- *d*, the difference between two pairs
- μ_d , the mean of these differences for the population

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n, the number of pairs of sample data

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The sample data must be matched pairs.

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- Either the differences must be normally distributed or the number of pairs must be larger than 30.

| Height P: | 189 | 173 | 183 | 180 | 179 |
|-----------|-----|-----|-----|-----|-----|
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We use StatCruch to calculate the differences and the test based on these differences. We want to test the hypothesis below.

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We use StatCruch to calculate the differences and the test based on these differences. We want to test the hypothesis below.

$$H_0: \mu_d = 0$$
$$H_1: \mu_d > 0$$

From StatCrunch, we get the differences.

| Height P: | 189 | 173 | 183 | 180 | 179 | |
|--------------|-----|-----|-----|-----|-----|--|
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| Differences: | 19 | -12 | 8 | 0 | 1 | |

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We also get a *P*-value of 0.2819, which tells us we should fail to reject our null hypothesis. This means our data does not support our original claim that presidents tend to be taller than their opponents.

Say you construct a 90% confidence interval for a the difference of two means, i.e. for $\mu_1 - \mu_2$ and that the confidence interval is (-0.5, -0.1), what can be said about the relationship between the two means?

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What's the difference between standard deviation and standard error?



The weights of 40 people are measured before and after a diet program, and the difference between their pre-program weight and postprogram weight is recorded. We want to test the claim that the mean weight lost is at least 2.1lbs. We conduct a 5% significance hypothesis test to test this claim and get a test statistic of -2.034. Does this support our claim or not? What's the difference between μ_d and \bar{d} ? When is μ_d the parameter under consideration as opposed to $\mu_1 - \mu_2$?
To test the hypothesis that the weight of a first-born twin is less than the weight of the second-born twin, would you consider μ_d or $\mu_1 - \mu_2$ in your null and alternative hypotheses?

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When conducting a critical value hypothesis test for a claim about $\mu_{d},$ what gets compared to the critical value?

- The Z-test statistic.
- The *T*-test statistic.
- The value set equal to μ_d in the null hypothesis.
- Any value that satisfies the inequality in the alternative hypothesis.

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The P-value.

Why must we require that there are at least five successes and five failures in each sample when conducting a hypothesis test concerning two proportions? What distributions are we actually comparing in these types of hypothesis tests?

You want to determine if the proportion of peas with adequate iron levels grown in water is less than the proportion of peas with adequate iron levels grown in soil. You sample 500 peas grown in water and 470 peas grown in soil. 45% of peas grown in water contain adequate amounts of iron and 45.2% of peas grown in soil contain adequate amounts of iron. Does this support the claim you wish to test or not?

Whether the average heights of longleaf pines and the average heights of loblolly pines are the same. You know that loblolly and longleaf pines vary in height by different amounts. A sample of 35 longleafs gives an average height of 75ft with standard deviation of 18 inches. A sample of 32 loblollies gives an average height of 75.1 feet with standard deviation of 11 inches. Do these samples support the claim that the average height of these pines is the same?