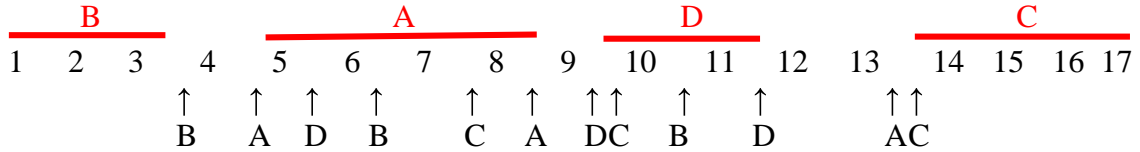




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4. [10] Four players (A, B, C, and D) are fairly dividing some items by the Method of Markers. They have marked the linear array below as shown. Describe the allocation of items to each player and indicate what items, if any, are leftover.



Leftover: 4, 9, 12, 13

5. [15] Three heirs, A, B, and C inherit two items from their uncle's estate: a piano and a painting. They decide to divide the items among themselves by the method of sealed bids. Their bids are in the bid table below. Complete the tables below and describe the final settlement, including what cash amounts each player has ultimately paid or gained.

Bids	Players			
Item	A	B	C	High Bidder
piano	\$6,750	\$8,000	\$6,000	<b>B</b>
painting	\$7,500	\$8,500	\$9,750	<b>C</b>
<b>Total Value</b>	<b>\$14,250</b>	<b>\$16,500</b>	<b>\$15,750</b>	
<b>Fair Share</b>	<b>\$4,750</b>	<b>\$5,500</b>	<b>\$5,250</b>	

Allocation				
Player	Item(s)	Value	Share	Put in (Take out)
A	none	\$0	\$4,750	Take out \$4,750
B	piano	\$8,000	\$5,500	Put in \$2,500
C	painting	\$9,750	\$5,250	Put in \$4,500
<b>Surplus</b>				<b>\$2,250</b>
<b>Share of Surplus</b>				<b>\$750</b>

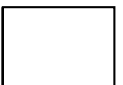
Describe the final settlement for each player below (including cash balance).

A: Gets no item, but get cash  $\$4,750 + \$750 = \$5,500$ .

B: Gets piano and pays  $\$2,500 - \$750 = \$1,750$ .

C: Gets painting and pays  $\$4,500 - \$750 = \$3,750$ .

Note that the cash paid and the cash received balance to \$0.

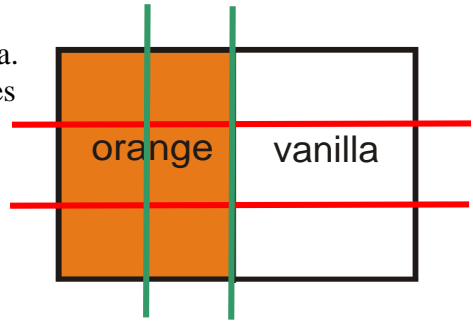




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8. [5] Assume that you like orange twice as much as vanilla. Divide the orange/vanilla cake illustrated into three pieces of equal value to you.

There are many correct answers. Two are shown, one in red (horizontal) cuts and one in green cuts.



9. [15] The legislature of a country has 140 seats to be apportioned among four states A, B, C, and D, in proportion to their populations. The table below shows the populations of the states. Complete the table by filling in **all** unshaded blanks in order to produce a Hamilton apportionment.

State	A	B	C	D	Total	Points
Population	90,642	32,648	150,070	6,640	280,000	2
Standard Divisor	2,000					3
Standard Quotas	45.321	16.324	75.035	3.320	140.000	3
Round Down	45	16	75	3	139	2
Surplus Seats	0	1	0	0	1	2
Hamilton App't	45	17	75	3	140	3

10. [5] In the legislative apportionment for Paradoxia, the states A, B, and C receive the apportionments A – 9 seats, B – 11 seats, and C – 5 seats, using Hamilton’s method with a house size of 150. The house size is increased to 151 but no populations change. When the apportionment is recalculated by the same method, the results are A – 10 seats, B – 12 seats and C – 4 seats. Why is this paradoxical and what paradox does this illustrate?

The paradox is that state C lost a seat even though the populations remained the same and a seat was added to the total. One would expect that C would retain its 5 seats and one lucky state would get the new seat as surplus seats were handed out. This is an example of the Alabama paradox.

