



# Nonradiative relaxation and inhomogeneous splitting of aggregated optical centers in the $\text{Nd}^{3+}$ -doped $\text{CaF}_2$ and $\text{SrF}_2$ crystals (FLN and decay study)

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## Abstract

Site-selective fluorescence and laser excitation spectroscopy for different types of optical centers in  $\text{SrF}_2 : \text{Nd}^{3+}$  (0.3 – 1.0%) and  $\text{SrF}_2 : \text{La}^{3+}$  (1.0%) :  $\text{Nd}^{3+}$  (0.2%) were performed at 4.2 K. The crystal-field levels of the  $^4\text{I}_{9/2}$ ,  $^4\text{F}_{3/2}$ , and  $^4\text{G}_{5/2}$  multiplets for different  $\text{Nd}^{3+}$  optical centers were determined in  $\text{SrF}_2 : \text{Nd}^{3+}$  (0.3%). An attempt was made to identify some of the new optical centers on the basis of their fluorescence lifetimes and crystal-field splitting. Some models of these centers have been discussed. Two–six times reduction of the  $^4\text{F}_{3/2}$  multiplet lifetime was observed in the pair M-center in comparison with the single optical centers due to energy cross-relaxation in the pair. A fine splitting of the levels at the  $^4\text{I}_{9/2}(1) \rightarrow ^4\text{G}_{5/2}(1)$  crystal-field transition ( $1.5 \text{ cm}^{-1}$ ) similar to that in  $\text{CaF}_2$  ( $2.4 \text{ cm}^{-1}$ ) was found for the Nd–Nd pair in  $\text{SrF}_2$ . The variation of the splitting from  $\text{CaF}_2$  to  $\text{SrF}_2$  nicely demonstrates the  $R^{-5}$  dependence of coherent quadrupole–quadrupole interaction. © 1999 Elsevier Science B.V. All rights reserved.

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## 1. Introduction

A fine resonance dynamical splitting at the  $^4\text{I}_{9/2}(1) \rightarrow ^4\text{G}_{5/2}(1)$  ( $\text{Z1} \rightarrow \text{D1}$ ) Stark–Stark transition in both the rhombic  $(\text{Nd}_{\text{Ca}}-\text{F}_i)_2$  pair M-center and in the trigonal  $(\text{Nd}_{\text{Ca}}-\text{F}_i)_4$  quartet N-center was previously found in the  $\text{CaF}_2 : \text{Nd}^{3+}$

crystals in the spectral domain by absorption spectroscopy [1] and in the time domain by coherent beating of the accumulated photon echo (APE) [2] at  $T = 10 \text{ K}$  and was confirmed by laser-induced site-selective time-resolved fluorescence spectroscopy at  $T = 4.2 \text{ K}$  [3]. Strong coherent quadrupole–quadrupole interaction between the  $\text{Nd}^{3+}$  ions inside the M and the N complexes was proposed as the reason for this splitting [1]. In contrast to  $\text{CaF}_2$  the aggregated  $\text{Nd}^{3+}$  centers in the  $\text{SrF}_2$  crystal have not been reliably identified

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before. The purpose of this work is to identify such clusters and to determine the energy diagram of the Stark levels for the ground  ${}^4I_{9/2}$  and the excited  ${}^4F_{3/2}$  and  ${}^4G_{5/2}$ ;  ${}^2G_{7/2}$  states for different  $Nd^{3+}$  centers in the  $SrF_2$  crystal. On the basis of these results we will try to compare the strength of coherent  $Nd^{3+}-Nd^{3+}$  interaction in the pair centers of  $SrF_2:Nd^{3+}$  crystal with the known values for  $CaF_2:Nd^{3+}$ .

## 2. Experimental results and discussion

The experimental set-up used in this study is described in our previous paper of the similar study in the  $CaF_2:Nd^{3+}$  crystals [3].

### 2.1. L-center with the single $Nd^{3+}$ ion

In the tetragonal symmetry L-center where the lattice  $Ca^{2+}$  cation is replaced by the impurity  $Nd^{3+}$  ion the charge-compensating fluorine  $F_i^-$  ion is located at the nearest to the rare-earth ion available interstitial position. The tetragonal symmetry of this center in  $CaF_2$  and  $SrF_2$  was established by EPR [4]. Fig. 1 presents inter-multiplet absorption spectra at the  ${}^4I_{9/2}(Z) \rightarrow {}^4F_{3/2}(R)$  transition for  $SrF_2:Nd^{3+}$  (0.3%),  $SrF_2:Nd^{3+}$  (1.0%),  $SrF_2:La^{3+}$  (1%): $Nd^{3+}$  (0.2%), and  $CaF_2:Nd^{3+}$  (0.2%) at  $T = 4.2$  K. One can see that along with the L-center there are many absorption lines of more complex centers. Comparison of the absorption spectra of  $SrF_2:Nd^{3+}$  (0.3%) and  $SrF_2:Nd^{3+}$  (1.0%) shows that the relative concentration of aggregated centers increases with increase in total neodymium concentration. At 1% of  $Nd^{3+}$  concentration the absorption line of the L-center in  $SrF_2$  is considerably stronger than in  $CaF_2$  due to the less-effective process of  $Nd^{3+}$  aggregation in the former one. The value of the Stark splitting of the  ${}^4F_{3/2}$  multiplet is found to be  $82\text{ cm}^{-1}$ , which is 1.4 times less than in  $CaF_2$ . The positions of the Stark levels of the  ${}^4I_{9/2}$ ,  ${}^4F_{3/2}$  and  ${}^4G_{5/2}$  multiplets in the L-center in the crystals in this study measured by absorption (Fig. 2) and laser fluorescence excitation (Fig. 3A) technique are in agreement with those reported in the earlier works [5,6]. The fluorescence lifetime measured at the  $R1 \rightarrow Z1$  transition

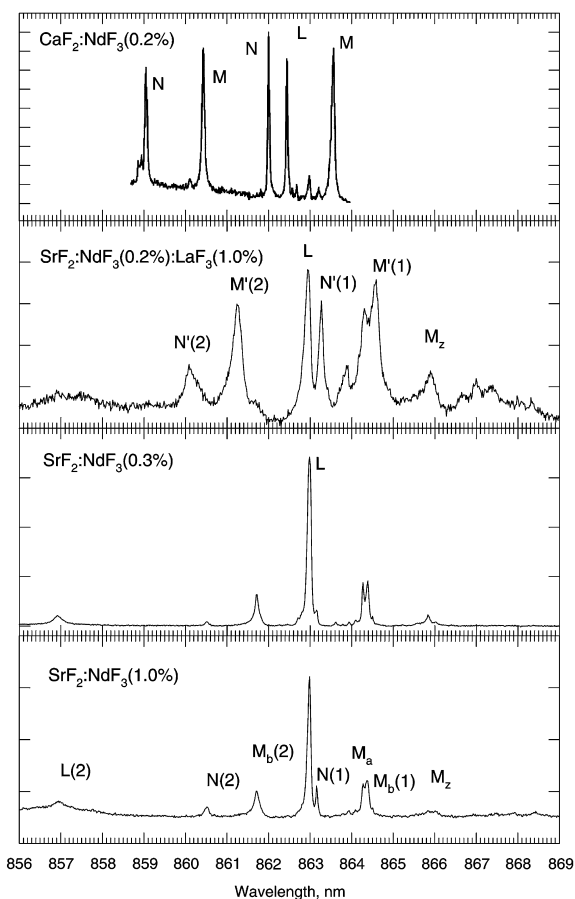


Fig. 1. Absorption spectra for  $CaF_2$  and  $SrF_2$  crystals for the  ${}^4I_{9/2} \rightarrow {}^4F_{3/2}$  transition of the  $Nd^{3+}$  ions at 4.2 K.

is 1.65 ms at  $T = 4.2$  K which is close to 1.7 ms measured at  $T = 10$  K [6].

## 3. Other optical centers

Weak clusterization in  $SrF_2$  did not allow earlier reliable identification of pair and other aggregated neodymium centers as was done in  $CaF_2$ . In doing so the absorption and fluorescence excitation spectra, as well as site-selective fluorescence kinetics decay were measured in  $SrF_2:Nd^{3+}$  crystals. In addition, we compared the data obtained for the well-known aggregated centers in  $CaF_2:Nd^{3+}$  (0.2%) and  $SrF_2:Nd^{3+}$  (1%) with the results for

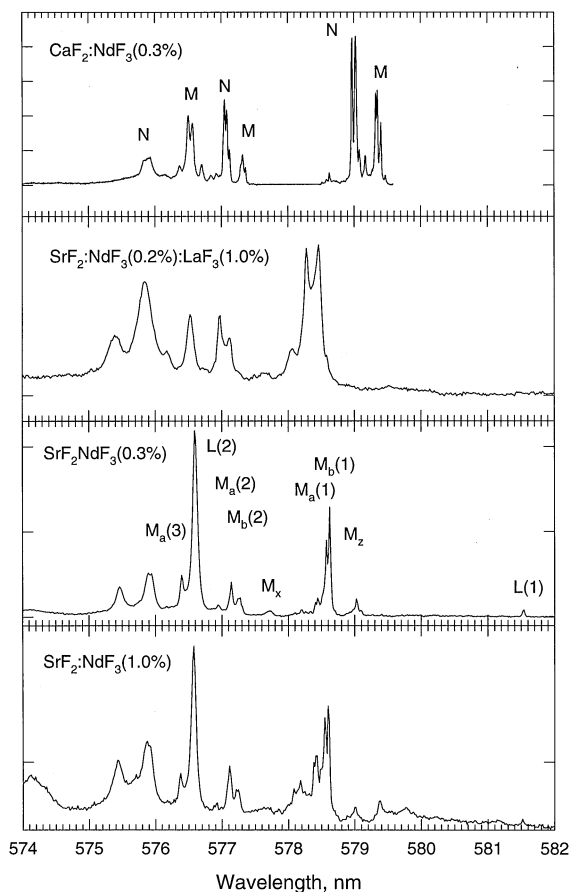


Fig. 2. Absorption spectra for  $\text{CaF}_2$  and  $\text{SrF}_2$  crystals for the  $^4I_{9/2} \rightarrow ^4G_{5/2}; ^2G_{7/2}$  transition of the  $\text{Nd}^{3+}$  ions at 4.2 K.

the mixed  $\text{SrF}_2 : \text{Nd}^{3+} (0.2\%) : \text{La}^{3+} (1.0\%)$  crystal. Fig. 1 shows the absorption spectra of these crystals at the  $^4I_{9/2} \rightarrow ^4F_{3/2}$  transition. Co-doping of the  $\text{Nd}^{3+}$ -doped fluorite-type crystals, for example with  $\text{La}^{3+}$ , leads to the formation of the  $M'$ -centers where one  $\text{Nd}^{3+}$  ion in the pair is substituted for optically inactive  $\text{La}^{3+}$ . Analysis of Fig. 1 shows that the formation of  $\text{La-Nd}$  complexes ( $M'$ -centers) in  $\text{SrF}_2$  is more effective than  $\text{Nd-Nd}$  ( $M$ -centers) ones. In addition, in  $\text{SrF}_2 : \text{Nd}^{3+} (0.2\%) : \text{La}^{3+} (1.0\%)$  the relative intensity of the  $L$ -centers absorption is considerably less than in  $\text{SrF}_2 : \text{Nd}^{3+} (1.0\%)$  for approximately the same total concentration of rare-earth dopants. As it was shown for  $\text{CaF}_2$  crystal [7] additional  $\text{La}^{3+}$

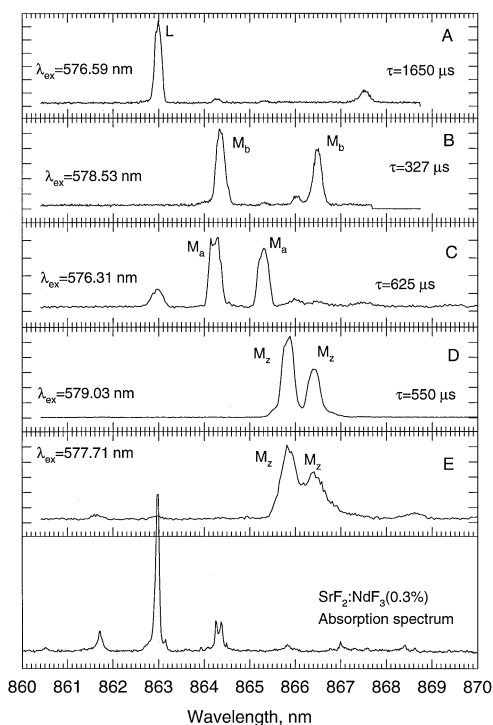


Fig. 3. Site-selective fluorescence spectra of the  $\text{SrF}_2 : \text{NdF}_3 (0.3\%)$  crystal for the  $^4F_{3/2}(1) \rightarrow ^4I_{9/2}(1,2)$  Stark-Stark transitions along with the absorption at the  $^4I_{9/2} \rightarrow ^4F_{3/2} (1,2)$  ones.

impurity leads to the increase in the total value of Stark splitting of the  $^4F_{3/2}$  multiplet of the  $M'$ -center with shifting of the higher  $^4F_{3/2}$  sublevel up and the lower one down. Using this fact and by comparing of  $\text{SrF}_2 : \text{Nd}^{3+}$  and  $\text{SrF}_2 : \text{Nd}^{3+} : \text{La}^{3+}$  absorption spectra we may identify  $N(1)$  and  $M_b(1)$  peaks as low Stark levels and  $M_b(2)$  and  $N(2)$  as a higher Stark levels of the  $^4F_{3/2}$  multiplet belonging to different centers. The distance between  $M_b(1)$  and  $M_b(2)$  lines is  $30 \text{ cm}^{-1}$  which is 1.4 times less than for the  $M$ -center in  $\text{CaF}_2$ . This result is similar to that found for the  $L$ -center in  $\text{CaF}_2$  and  $\text{SrF}_2$  where this ratio is also 1.4. There is no energy shift of the  $M_z$  absorption bands in  $\text{SrF}_2 : \text{Nd}^{3+} (0.2\%) : \text{LaF}_3 (1.0\%)$  and  $\text{SrF}_2 : \text{Nd}^{3+}$  found. This allows to propose that this type of center is a single rare-earth impurity center which could differ from the  $L$ -center by the way of charge compensation (analog of  $Y$ -center in  $\text{CaF}_2$  [7] when the extra

charge of  $\text{Nd}^{3+}$  is compensated by two  $\text{F}_i^-$  in the first or in the second coordination sphere or by one  $\text{F}_i^-$  in the second sphere [8]).

### 3.1. $M_b$ -center

Absorption spectra of the  ${}^4\text{I}_{9/2} \rightarrow {}^4\text{G}_{5/2}$ ;  ${}^2\text{G}_{7/2}$  transition for the crystals studied are shown in Fig. 2. Fluorescence spectra from the  ${}^4\text{F}_{3/2}$  multiplet of  $\text{Nd}^{3+}$  optical centers with excitation into the  ${}^4\text{G}_{5/2}$  multiplet are presented in Fig. 3. Three fluorescence spectral lines with maxima at 864.3, 866.4 (Fig. 3B) and 873.9 nm obtained under 578.53 nm excitation associated with transitions of the  $M_b$ -center from the lower lying Stark level of the  ${}^4\text{F}_{3/2}$  multiplet to the first, second, and third Stark levels of the ground  ${}^4\text{I}_{9/2}$  multiplet were registered. The measured Stark energy levels positions for this  $M_b$ -center (Table 1) are very close to the results of work [6]. The measured fluorescence lifetime (Table 2) was found to be four times larger at 4.2 K ( $\tau = 327 \mu\text{s}$ ) in  $\text{SrF}_2 : \text{Nd}^{3+}$  than for the pair (Nd–Nd) M-centers in  $\text{CaF}_2$  ( $\tau = 79 \mu\text{s}$ ). According to Han et al. [6] the fluorescence lifetime of the  $M_b$ -centers in  $\text{SrF}_2 : \text{Nd}^{3+}$  at 10 K is 237  $\mu\text{s}$  whereas at 77 K it was found even shorter at 105.6  $\mu\text{s}$  [9]. Previously, the lifetime shortening with temperature was observed for the M-pair (Nd–Nd) center in  $\text{CaF}_2$  [10]. Using the results of this work the quenching energy transfer rates from the  ${}^4\text{F}_{3/2}$  multiplet in the Nd–Nd pair in  $\text{CaF}_2$  could be determined at different temperatures. In the range of 4.2–10 K it was found to be constant ( $W_0 = 8877 \text{ s}^{-1}$ ). Knowing the energy transfer rate

Table 1  
Energy levels positions ( $\text{cm}^{-1}$ ) for different optical centers in the  $\text{SrF}_2$  (0.3%):  $\text{Nd}^{3+}$  crystal obtained from absorption, excitation and fluorescence spectra at 4.2 K

Center type		L	$M_a$	$M_z$	$M_b$
${}^4\text{I}_{9/2}$	Z1	0	0	0	0
	Z2	57	13	7	28
	Z3	153	110		127
${}^4\text{F}_{3/2}$	R1	11 584	11 569	11 550	11 567
	R2	11 667			11 597
${}^4\text{G}_{5/2}$	D1	17 197	17 282	17 270	17 284
	D2	17 343	17 327	17 328	17 324

Table 2

Fluorescence lifetime of the  ${}^4\text{F}_{3/2}$  multiplet for different optical centers in  $\text{SrF}_2 : \text{Nd}^{3+}$

Center type	Life time, $\mu\text{s}$ (TK)
L	1650 (4.2 K) <sup>a</sup>
	1700 (10 K) [6]
	325 (4.2 K) <sup>a</sup>
$M(M_6)$	237 (10 K) [6]
	105.6 (77 K) [9]
$M_a$	615 (4.2 K) <sup>a</sup>
$M_z$	550 (4.2 K) <sup>a</sup>

<sup>a</sup>Result of this paper.

in the pair we could determine the  $C_{\text{DA}}$  – micro-efficiency of energy transfer (as  $C_{\text{DA}} = W_0 \times R_{\text{min}}^6$ ) if we know the Nd–Nd distance in the pair. In [8] the positions of the  $\text{La}^{3+}$  ions and interstitial fluorine ions ( $\text{F}_i^-$ ) in the La–La pair in  $\text{CaF}_2$  and  $\text{SrF}_2$  were determined theoretically in the configuration of minimum energy. As the ionic radii are very close for  $\text{Nd}^{3+}$  and  $\text{La}^{3+}$  we used these results for estimation of the distance in the Nd–Nd pair in these crystals. They were found to be 0.364 and 0.396 nm for  $\text{CaF}_2$  and  $\text{SrF}_2$  crystals, respectively. According to Basiev et al. [11] the dipole–dipole interaction is dominant in the nonradiative energy transfer if the squares of the reduced matrix elements  $U^{(4)}$  and  $U^{(6)}$  are much higher than the squares of  $U^{(2)}$  for both the donor and acceptor transitions involved. This condition is fulfilled for the cross-relaxation from the  ${}^4\text{F}_{3/2}$  state since the matrix elements  $U^{(2)}$  for all electronic transitions participating in the process are equal or close to zero. With this in mind we estimated  $C_{\text{DA}}$  micro-parameters at different temperatures in the  $\text{CaF}_2 : \text{Nd}^{3+}$  and  $\text{SrF}_2 : \text{Nd}^{3+}$  crystals. The result of these calculations in the pair M-center in  $\text{CaF}_2$  and  $\text{SrF}_2$  are presented in Table 3. It is seen that the value of  $C_{\text{DA}}$  increases for both the crystals when the temperature rises. According to Voron'ko et al. [10] the fluorescence of the M-center in  $\text{CaF}_2 : \text{Nd}^{3+}$  at  $T = 77 \text{ K}$  is quenched completely. This is an indication of phonon-assisted resonance energy transfer and deals with the increase in temperature of the overlap integral of the donor (excited  $\text{Nd}^{3+}$  ion) fluorescence spectrum and absorption spectrum of acceptor (the second unexcited ion of the

Table 3

The  $C_{DA}/10^{-41}$  (cm<sup>6</sup>/s) — micro-parameter of the nonradiative energy transfer from the  ${}^4F_{3/2}$  multiplet of the  $Nd^{3+}$  ion in the pair M-centers in the  $CaF_2$  and  $SrF_2$  crystals

T(K)	4.2	10	77
$CaF_2$	2.07 [10], 2.6 [3]	2.07 [10], 2.14 [5]	
$SrF_2$	0.523 <sup>a</sup>	0.897 [5]	3.013 [9]

<sup>a</sup>Result of this paper.

Nd–Nd pair). The larger values of  $C_{DA}$  in  $CaF_2$  in comparison with  $SrF_2$  may be related to the larger overlap integrals of electronic resonances of donors and acceptors because of different values of Stark splitting. The larger lifetimes of the  ${}^4F_{3/2}$  manifold of the pair M-center in  $SrF_2$  in comparison with  $CaF_2$  is caused by larger minimal distance (Nd–Nd) and the smaller values of the  $C_{DA}$  micro-parameters in  $SrF_2$ .

### 3.2. $M_a$ - and $M_z$ -centers

The fluorescence of the  $M_a$ -center is more pronounced when we excite the third Stark level of the  ${}^4G_{5/2}$ ,  ${}^2G_{7/2}$  multiplet at 576.31 nm (Fig. 3C).

The fluorescence of the  $M_z$ -center is more pronounced when we excite at 579.03 nm into the lowest Stark level of the  ${}^4G_{5/2}$ ,  ${}^2G_{7/2}$  multiplet (Fig. 3D). This center exhibits rather low value of Stark splitting of the ground  ${}^4I_{9/2}$  multiplet suggesting low values of the even crystal-field parameters. The Stark energy level positions of the ground  ${}^4I_{9/2}$  multiplet obtained for the  $M_a$  and the  $M_z$  centers after the fluorescence spectra analysis are presented in Table 1. The fluorescence lifetime of the  $M_z$ -center (550  $\mu$ s) is quite close to that of the  $M_a$ -center (615  $\mu$ s) (see Table 2). If our presumption that the  $M_z$ -center is the single center with the compensation of an extra charge of  $Nd^{3+}$  ion by two interstitial  $F_i^-$  ions spaced in the first or in the second coordination sphere (like Y-center in  $CaF_2$ ) or by one  $F_i^-$  in the second sphere is correct; then its lifetime reduction can be connected with the increase in the radiative rate due to higher values of the odd crystal-field parameters in comparison with those for the L-center. The same can be true for the  $M_a$ -center. There is good indirect evidence

of the discussed nature of these two centers. Theoretical calculations of work [8] show that the energy change in forming the  $La^{3+}-F_i^-$  complex from an isolated ion and interstitial fluorine ion in the second coordination sphere is larger in  $SrF_2 : La^{3+}$  than in  $CaF_2 : La^{3+}$ . And vice versa, the energy change on forming the  $La^{3+}-F_i^-$  complex with an interstitial fluorine in the first coordination sphere is larger for  $CaF_2 : La^{3+}$  than for  $SrF_2 : La^{3+}$ . This can prove the lack of the  $M_a$  and  $M_z$  complex centers in  $CaF_2 : Nd^{3+}$  and their existence in  $SrF_2 : Nd^{3+}$ .

Fluorescence of the  $M_z$ -center (Fig. 3E) was observed also using 577.71 nm excitation into the  $M_x$  absorption band (Fig. 2). However, the pronounced build-up of the  $M_z$ -center fluorescence decay with this excitation shows that the  $M_x$  absorption band belongs to another optical center. An effective nonradiative energy transfer to the  $M_z$ -center could be proposed as a reason for this build-up.

### 4. Fine levels splitting of pair centers

The maximum value of a fine dynamical splitting up to 2.4 cm<sup>-1</sup> for the Z1 → D1 crystal field Stark–Stark transition of the pair M-center of  $Nd^{3+}$  in  $CaF_2$  was found in Refs. [1–3,12] using time resolved site-selective fluorescence spectroscopy, photon echo and selective laser-saturation spectroscopy. It was shown theoretically in Ref. [1] that the fine dynamical splitting is caused by resonance electric quadrupole–quadrupole interaction between  $Nd^{3+}$  ions in the pair. For this interaction the fine splitting is proportional to  $\Delta = e^2 \langle r^2 \rangle^2 / R_{min}^5 |(J||U^{(2)}||J)|^2$ , where  $\langle r^2 \rangle$  is the square of the 4f electronic radius averaged over the 4f-wave function. This type of interaction is maximal for the  ${}^4G_{5/2}$  multiplet as the reduced matrix element ( ${}^4I_{9/2} || U^2 || {}^4G_{5/2}$ ) = 0.897 [13] is extremely large compared to those from the ground state to other excited multiplets ( $({}^4I_{9/2} || U^2 || {}^{2S+1}L_J) < 0.1$ ). The theoretical analysis gives the value of the splitting equal to 1–7 cm<sup>-1</sup> which is close to the experimental data. For the determination of the fine splitting of the pair center in  $SrF_2$  we studied the excitation spectra of the  $M_b$ -centers with

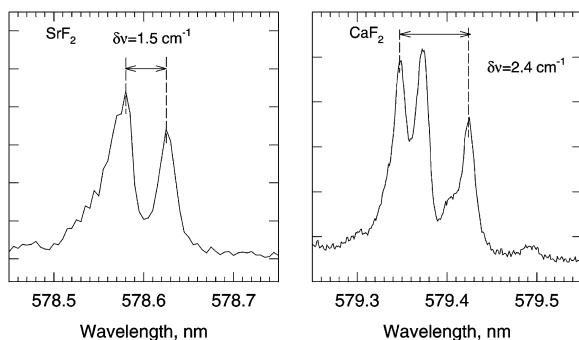


Fig. 4. Dynamical fine-splitting of the  ${}^4I_{9/2}(1) \rightarrow {}^4G_{5/2}(1)$  Stark–Stark transition due to quadrupole–quadrupole interaction in the Nd–Nd pair M-center in  $\text{CaF}_2$  and  $\text{SrF}_2$  crystals.

fluorescence registration at 866.4 nm ( $R1 \rightarrow Z2$  transition). The result (Fig. 4) demonstrates a fine splitting of  $R1 \rightarrow D1$  crystal-field transition of the  $M_b$ -center with the value of  $1.5 \text{ cm}^{-1}$ . The reason for this expected reduction in the value of the dynamical splitting from  $\text{CaF}_2$  to  $\text{SrF}_2$  is the increase in the lattice parameters in  $\text{SrF}_2$  in comparison with  $\text{CaF}_2$ . The following ratios confirm the  $R^{-5}$  dependence of the measured values of the fine splitting, which is indicative of coherent quadrupole–quadrupole interaction in the Nd–Nd pair:

$$\frac{\Delta(\text{CaF}_2)}{\Delta(\text{SrF}_2)} = \frac{2.4 \text{ cm}^{-1}}{1.5 \text{ cm}^{-1}} = 1.60,$$

$$\frac{R_{\min}^5(\text{SrF}_2)}{R_{\min}^5(\text{CaF}_2)} = \frac{(0.396 \text{ nm})^5}{(0.364 \text{ nm})^5} = 1.52,$$

where  $R_{\min}(\text{SrF}_2)$  and  $R_{\min}(\text{CaF}_2)$  is the minimum distance between the Nd ions in the pair.

## 5. Conclusion

Site-selective fluorescence and laser excitation study of the  $\text{SrF}_2:\text{Nd}^{3+}$  (0.3–1.0%) and  $\text{SrF}_2:\text{La}^{3+}$  (1.0%): $\text{Nd}^{3+}$  (0.2%) crystals at 4.2 K has identified Stark-level energy positions of different optical centers. Two–six times reduction of the  ${}^4F_{3/2}$  multiplet lifetime was observed in the pair M-center in comparison with the single optical centers due to dipole–dipole quenched energy transfer in the Nd–Nd pair. Slower energy transfer rate from the  ${}^4F_{3/2}$  multiplet of the M-center in  $\text{SrF}_2$  in

comparison with  $\text{CaF}_2$  is caused by larger minimal distance (Nd–Nd) and by the smaller values of the  $C_{\text{DA}}$  micro-parameter in  $\text{SrF}_2$ .

A fine splitting for the  ${}^4I_{9/2}(1) \rightarrow {}^4G_{5/2}(1)$  Stark–Stark transition of the  $\text{Nd}^{3+}$  pair center was found to be  $\Delta = 1.5 \text{ cm}^{-1}$  in  $\text{SrF}_2$  similar to the dynamical splitting for the  $\text{Nd}^{3+}$  pairs in  $\text{CaF}_2$  ( $\Delta = 2.4 \text{ cm}^{-1}$ ). The reduction in the value of fine splitting from  $\text{CaF}_2$  to  $\text{SrF}_2$  demonstrates the  $R^{-5}$  dependence predicted for coherent quadrupole–quadrupole interaction and proves the dynamical character of this splitting.

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