

MA 587/687

Name (Print last name first):

Quiz 3

Question 1Suppose the joint pmf $p(x, y, z)$ of X, Y, Z is given by

$$p(1, 1, 1) = 1/3, p(1, 1, 2) = 1/18, p(1, 2, 1) = 1/18, p(1, 2, 2) = 1/16$$

$$p(2, 1, 1) = 1/18, p(2, 1, 2) = 1/16, p(2, 2, 1) = 1/4, p(2, 2, 2) = 1/8.$$

What is $E(Y|Z = 1)$? What is $E(X|Y = 1, Z = 2)$?Question 2

A prisoner is trapped in a cell with 3 doors. The first door returns to his cell after 3 days. The second returns to his cell after 4 days. The third leads to freedom after 5 days of travel. Assuming he chooses the doors (independently each time, because he doesn't learn) with $p_1 = 1/6, p_2 = 1/3, p_3 = 1/2$, what is the expected number of days until freedom?